

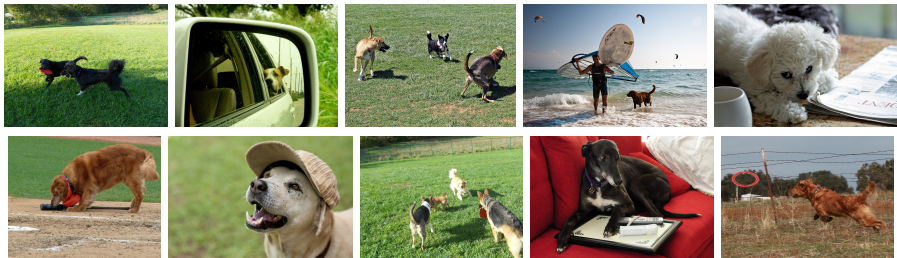
Computer vision - Retrieval

Ronan Sifre

Credits to Yannis Avrithis <https://sif-dlv.github.io/>

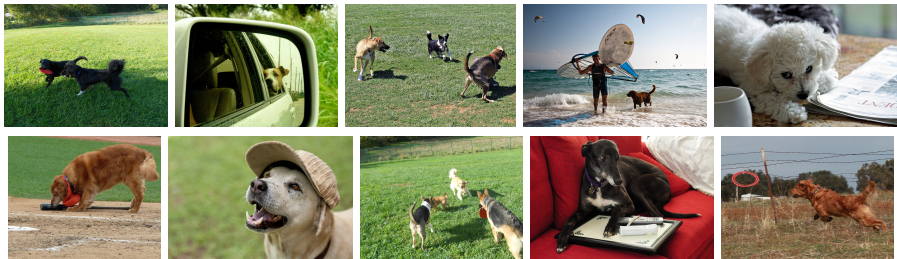
background

image classification challenges



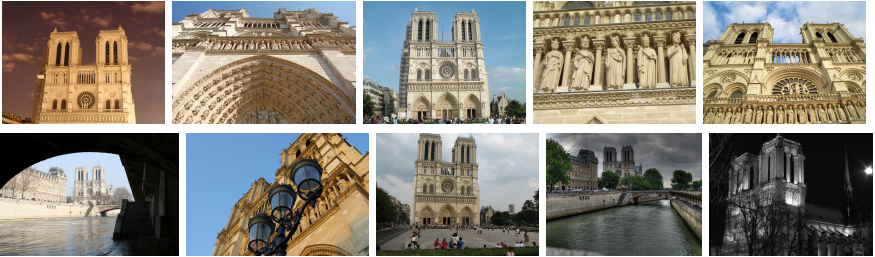
- scale
- viewpoint
- occlusion
- clutter
- lighting
- number of instances
- texture/color
- pose
- deformability
- intra-class variability

image classification challenges



- scale
- viewpoint
- occlusion
- clutter
- lighting
- number of instances
- texture/color
- pose
- deformability
- intra-class variability

image retrieval challenges



- scale
- viewpoint
- occlusion
- clutter
- lighting

- distinctiveness
- distractors

main difference to classification:

- no intra-class variability

image retrieval challenges



- scale
- viewpoint
- occlusion
- clutter
- lighting

- distinctiveness
- distractors

main difference to classification:

- no intra-class variability

image retrieval challenges



- scale
- viewpoint
- occlusion
- clutter
- lighting

- distinctiveness
- distractors

main difference to classification:

- no intra-class variability

vector quantization → visual words



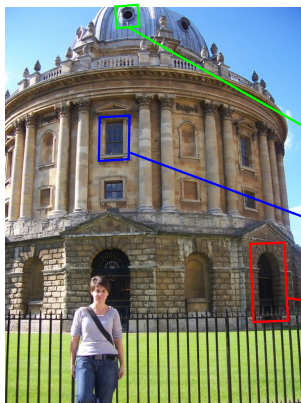
query



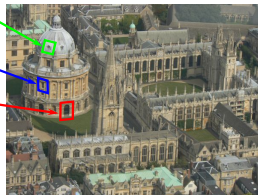
15

- query vs. dataset image

vector quantization \rightarrow visual words



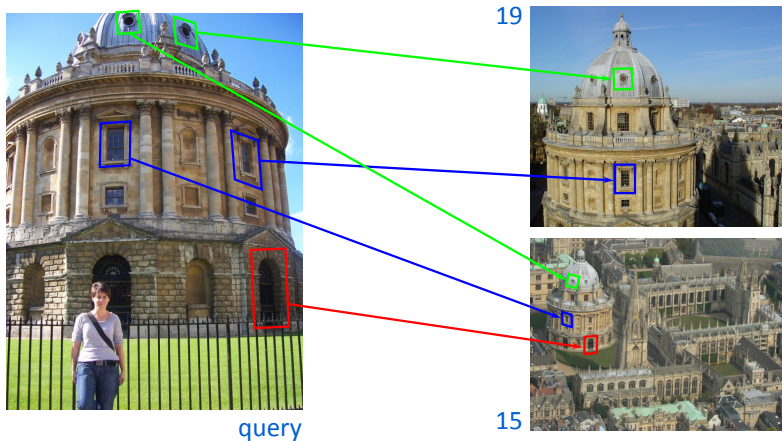
query



15

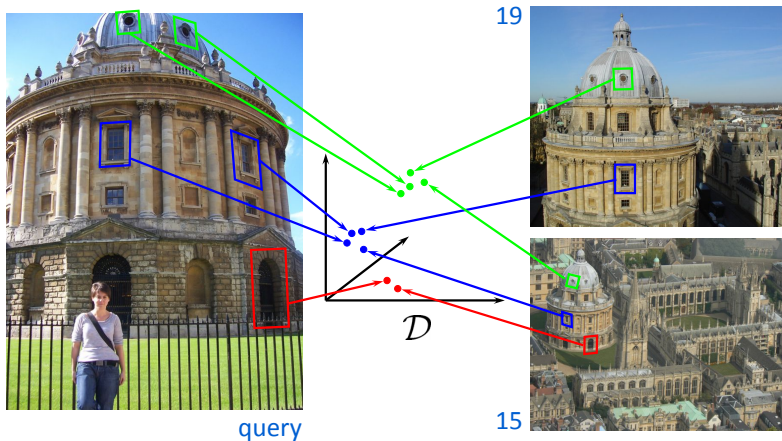
- pairwise descriptor matching

vector quantization → visual words



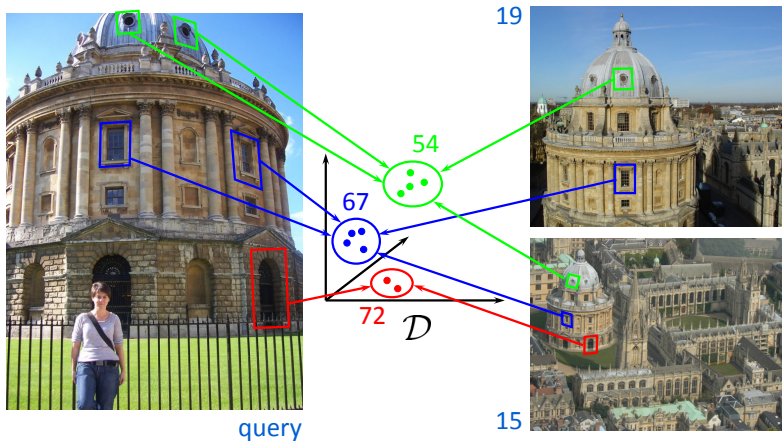
- pairwise descriptor matching for **every** dataset image

vector quantization \rightarrow visual words



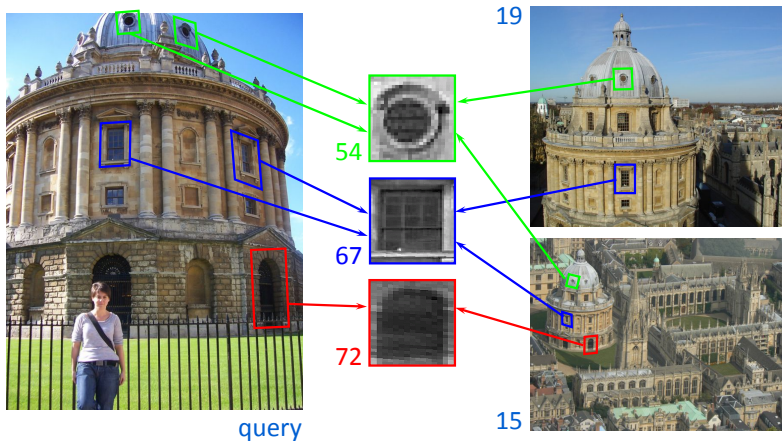
- similar descriptors should all be nearby in the descriptor space

vector quantization \rightarrow visual words



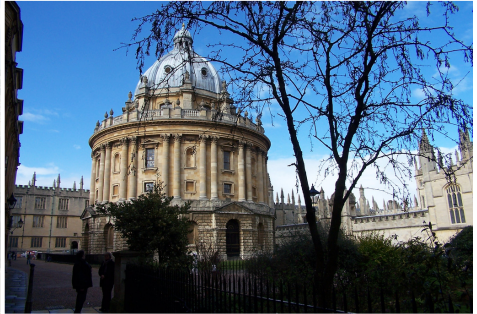
- let's quantize them into visual words

vector quantization → visual words



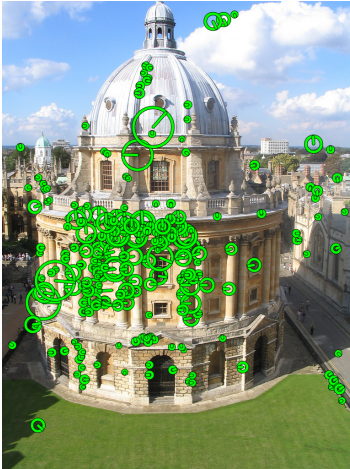
- now visual words act as a proxy; no pairwise matching needed

back to geometry: re-ranking



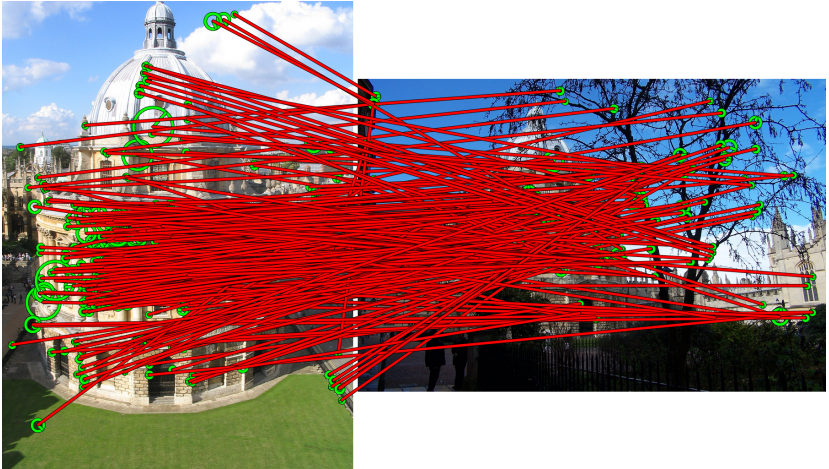
original images

back to geometry: re-ranking



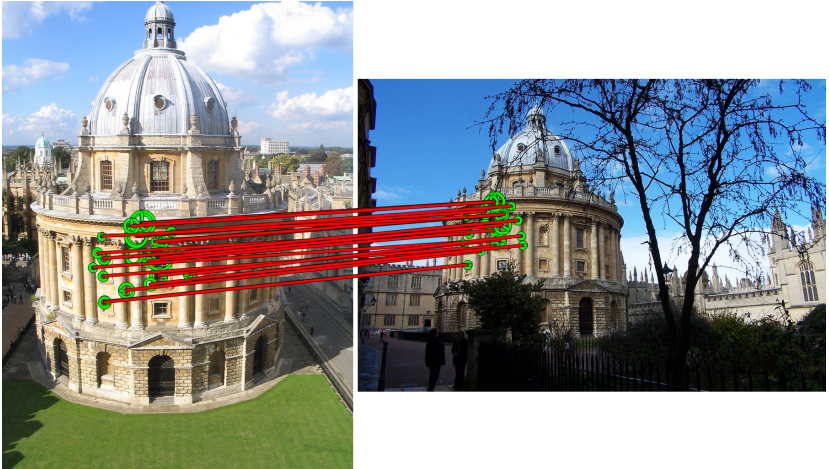
local features

back to geometry: re-ranking



tentative correspondences: too many

back to geometry: re-ranking

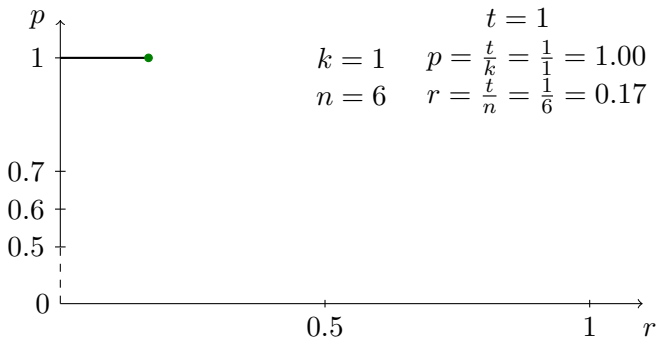


inliers: now more expensive to find

average precision (AP)

- ranked list of items with true/false labels

1	2	3	4	5	6	7	8	9	10	11	12
T	T	F	T	F	F	T	F	T	T	F	F

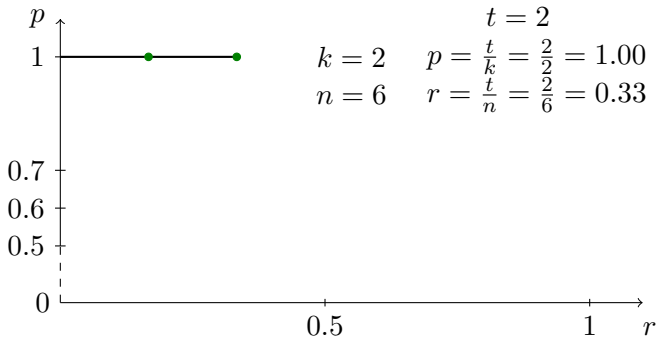


- # total ground truth n , current rank k , # true positives t
- precision $p = \frac{t}{k}$, recall $r = \frac{t}{n}$

average precision (AP)

- ranked list of items with true/false labels

1	2	3	4	5	6	7	8	9	10	11	12
T	T	F	T	F	F	T	F	T	T	F	F

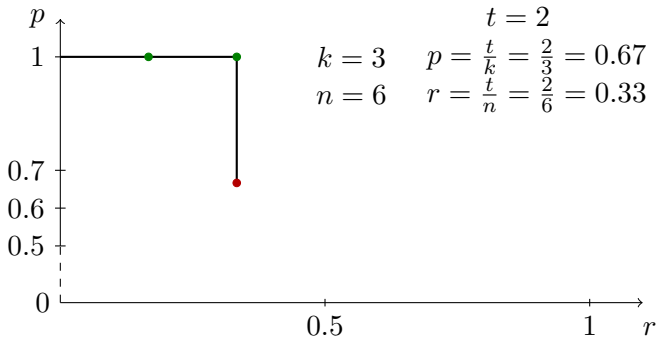


- # total ground truth n , current rank k , # true positives t
- precision $p = \frac{t}{k}$, recall $r = \frac{t}{n}$

average precision (AP)

- ranked list of items with true/false labels

1	2	3	4	5	6	7	8	9	10	11	12
T	T	F	T	F	F	T	F	T	T	F	F

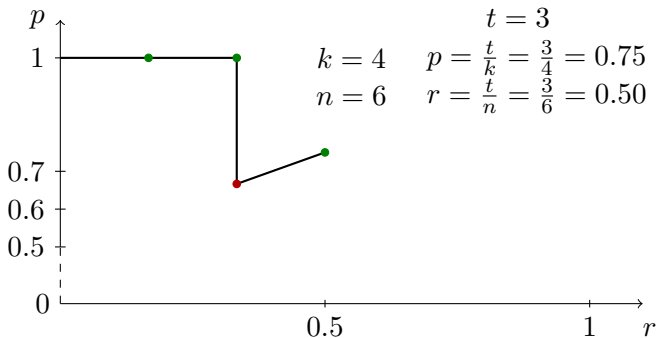


- # total ground truth n , current rank k , # true positives t
- precision $p = \frac{t}{k}$, recall $r = \frac{t}{n}$

average precision (AP)

- ranked list of items with true/false labels

1	2	3	4	5	6	7	8	9	10	11	12
T	T	F	T	F	F	T	F	T	T	F	F

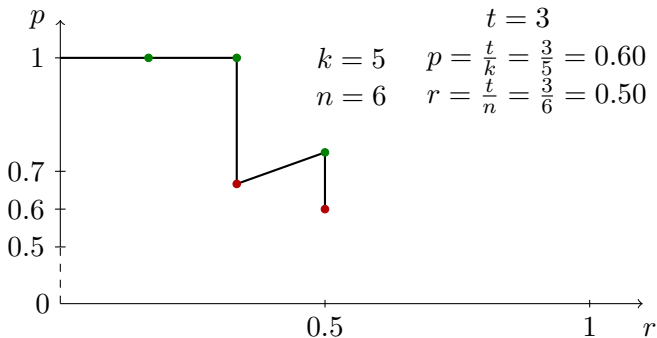


- # total ground truth n , current rank k , # true positives t
- precision $p = \frac{t}{k}$, recall $r = \frac{t}{n}$

average precision (AP)

- ranked list of items with true/false labels

1	2	3	4	5	6	7	8	9	10	11	12
T	T	F	T	F	F	T	F	T	T	F	F

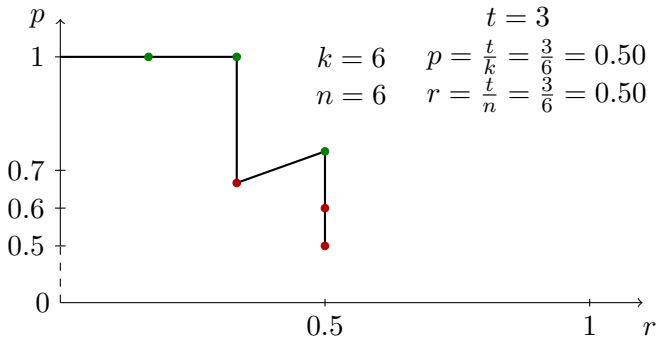


- # total ground truth n , current rank k , # true positives t
- precision $p = \frac{t}{k}$, recall $r = \frac{t}{n}$

average precision (AP)

- ranked list of items with true/false labels

1	2	3	4	5	6	7	8	9	10	11	12
T	T	F	T	F	F	T	F	T	T	F	F

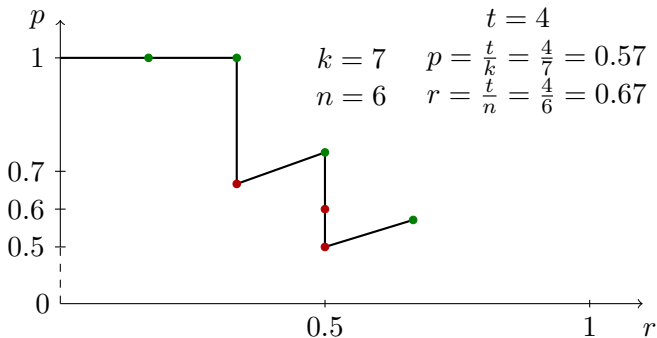


- # total ground truth n , current rank k , # true positives t
- precision $p = \frac{t}{k}$, recall $r = \frac{t}{n}$

average precision (AP)

- ranked list of items with true/false labels

1	2	3	4	5	6	7	8	9	10	11	12
T	T	F	T	F	F	T	F	T	T	F	F

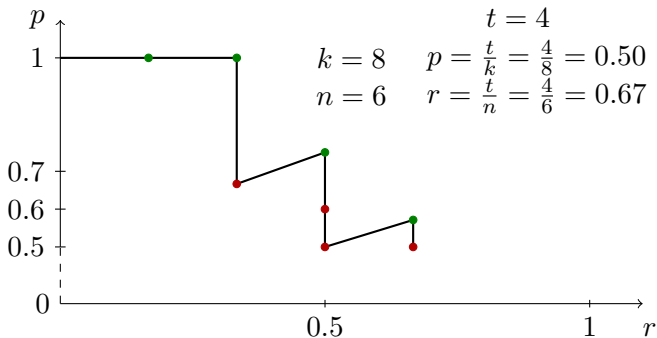


- # total ground truth n , current rank k , # true positives t
- precision $p = \frac{t}{k}$, recall $r = \frac{t}{n}$

average precision (AP)

- ranked list of items with true/false labels

1	2	3	4	5	6	7	8	9	10	11	12
T	T	F	T	F	F	T	F	T	T	F	F

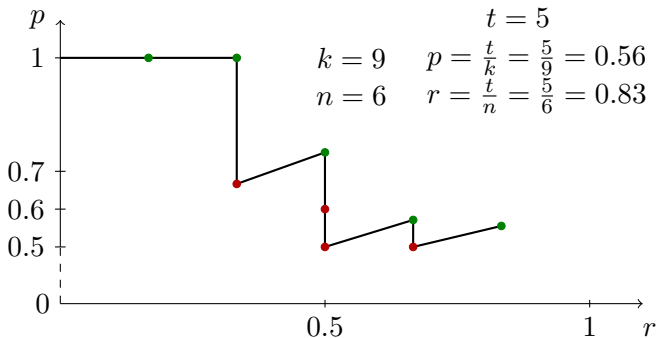


- # total ground truth n , current rank k , # true positives t
- precision $p = \frac{t}{k}$, recall $r = \frac{t}{n}$

average precision (AP)

- ranked list of items with true/false labels

1	2	3	4	5	6	7	8	9	10	11	12
T	T	F	T	F	F	T	F	T	T	F	F

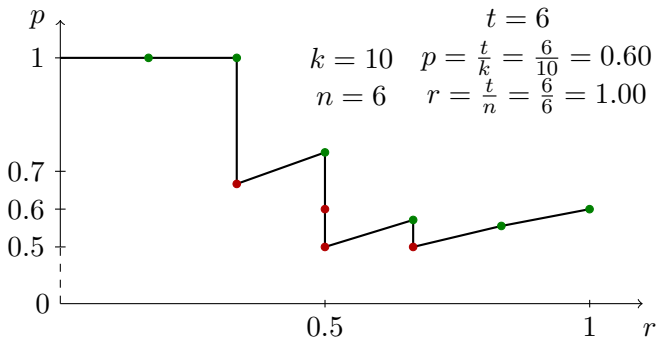


- # total ground truth n , current rank k , # true positives t
- precision $p = \frac{t}{k}$, recall $r = \frac{t}{n}$

average precision (AP)

- ranked list of items with true/false labels

1	2	3	4	5	6	7	8	9	10	11	12
T	T	F	T	F	F	T	F	T	T	F	F

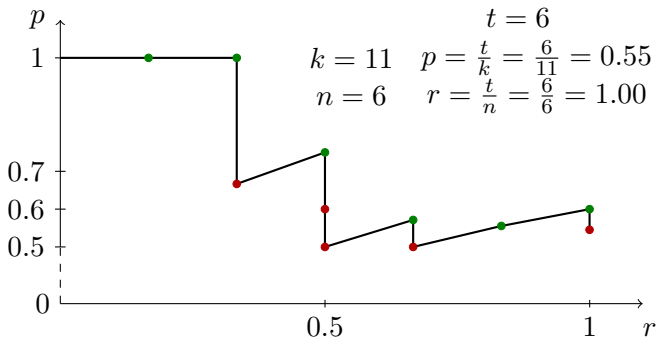


- # total ground truth n , current rank k , # true positives t
- precision $p = \frac{t}{k}$, recall $r = \frac{t}{n}$

average precision (AP)

- ranked list of items with true/false labels

1	2	3	4	5	6	7	8	9	10	11	12
T	T	F	T	F	F	T	F	T	T	F	F

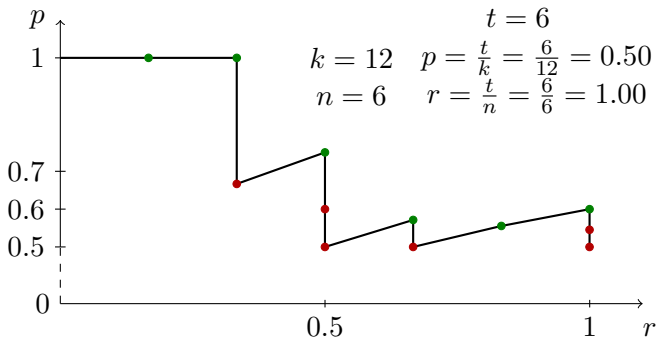


- # total ground truth n , current rank k , # true positives t
- precision $p = \frac{t}{k}$, recall $r = \frac{t}{n}$

average precision (AP)

- ranked list of items with true/false labels

1	2	3	4	5	6	7	8	9	10	11	12
T	T	F	T	F	F	T	F	T	T	F	F

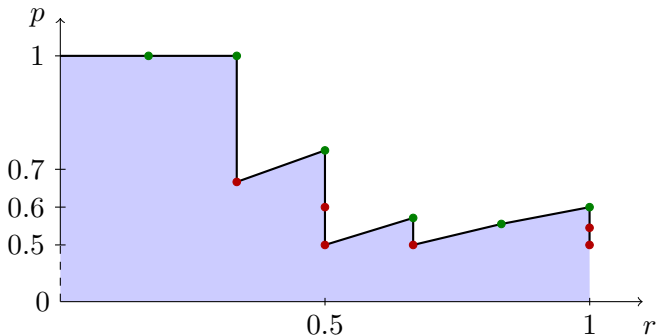


- # total ground truth n , current rank k , # true positives t
- precision $p = \frac{t}{k}$, recall $r = \frac{t}{n}$

average precision (AP)

- ranked list of items with true/false labels

1	2	3	4	5	6	7	8	9	10	11	12
T	T	F	T	F	F	T	F	T	T	F	F

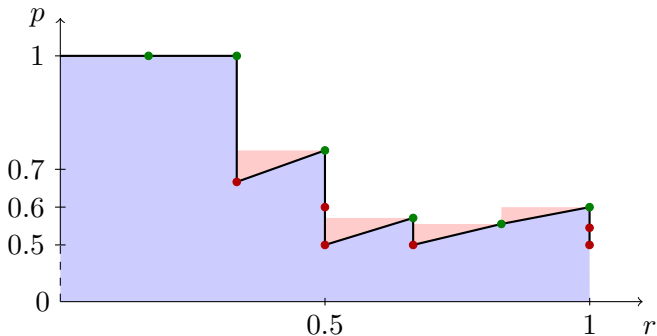


- average precision = area under curve
- the mean average precision (mAP) is the mean over queries

average precision (AP)

- ranked list of items with true/false labels

1	2	3	4	5	6	7	8	9	10	11	12
T	T	F	T	F	F	T	F	T	T	F	F



- average precision = area under curve (filled-in curve)
- the mean average precision (mAP) is the mean over queries

Oxford buildings dataset

[Philbin et al. 2007]



All Souls



Ashmolean



Balliol



Bodleian



Christ Church



Cornmarket



Hertford



Keble



Magdalen



Pitt Rivers



Radcliffe Camera

- **Oxford5k**: 5k images, 11 landmarks, $5 \times 11 = 55$ queries, 10 ~ 200 positives/query
- **Oxford105k**: 100k additional **distractor** images

Paris dataset

[Philbin et al. 2008]



Defense



Eiffel



Invalides



Louvre



Moulin Rouge



Musée d'Orsay



Notre Dame



Pantheon



Pompidou



Sacré-Cœur

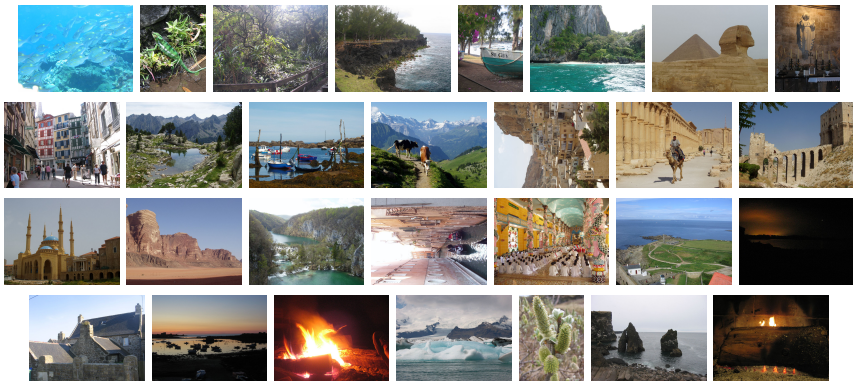


Triomphe

- **Paris6k**: 6k images, 11 landmarks, $5 \times 11 = 55$ queries, $50 \sim 300$ positives/query
- **Paris106k**: same 100k **distractor** images as Oxford

Holidays dataset

[Jégou et al. 2008]



- personal holiday photos, natural and man-made scenes
- 1.5k images, 500 groups, 1 query/group, 1000 positives, 1 ~ 12 positives/query

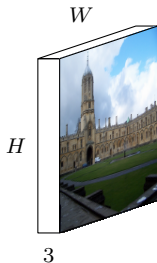
neural codes for image retrieval



- **fine-tuning** by softmax on 672 classes of 200k landmark photos
- outperforms VLAD and Fisher vectors on standard retrieval benchmarks, but still inferior to SIFT local descriptors

regional CNN features

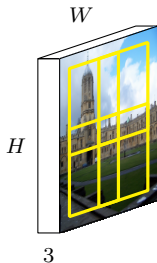
[Razavian et al. 2015]



- 3-channel RGB input, largest square region extracted
- fixed multiscale overlapping regions, warped into $w \times h = 227 \times 227$
- each region yields a $w' \times h' \times k = 36 \times 36 \times 256$ dimensional feature at the last convolutional layer of AlexNet
- global spatial max-pooling
- ℓ_2 -normalization, PCA-whitening of each descriptor

regional CNN features

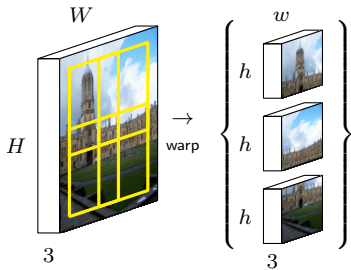
[Razavian et al. 2015]



- 3-channel RGB input, largest square region extracted
- fixed multiscale overlapping regions, warped into $w \times h = 227 \times 227$
- each region yields a $w' \times h' \times k = 36 \times 36 \times 256$ dimensional feature at the last convolutional layer of AlexNet
- global spatial max-pooling
- ℓ_2 -normalization, PCA-whitening of each descriptor

regional CNN features

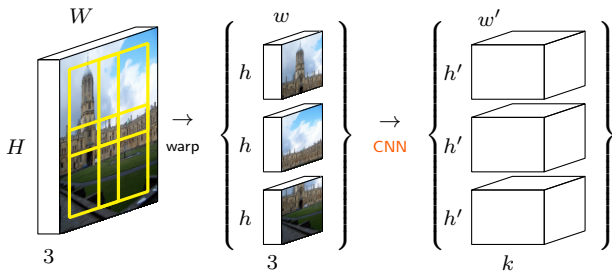
[Razavian et al. 2015]



- 3-channel RGB input, largest square region extracted
- fixed multiscale overlapping regions, **warped** into $w \times h = 227 \times 227$
- **each region** yields a $w' \times h' \times k = 36 \times 36 \times 256$ dimensional feature at the last convolutional layer of AlexNet
- global spatial **max**-pooling
- ℓ_2 -normalization, PCA-whitening of each descriptor

regional CNN features

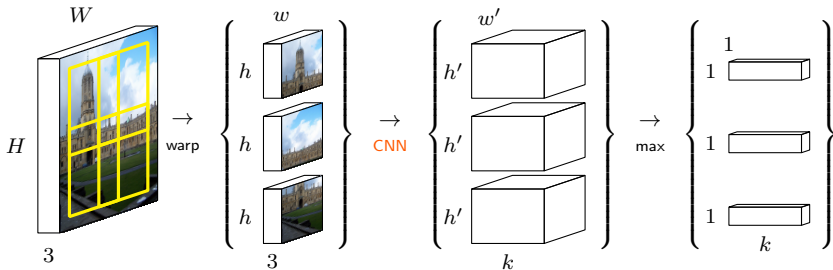
[Razavian et al. 2015]



- 3-channel RGB input, largest square region extracted
- fixed multiscale overlapping regions, **warped** into $w \times h = 227 \times 227$
- **each region** yields a $w' \times h' \times k = 36 \times 36 \times 256$ dimensional feature at the last convolutional layer of AlexNet
- global spatial **max**-pooling
- ℓ_2 -normalization, PCA-whitening of each descriptor

regional CNN features

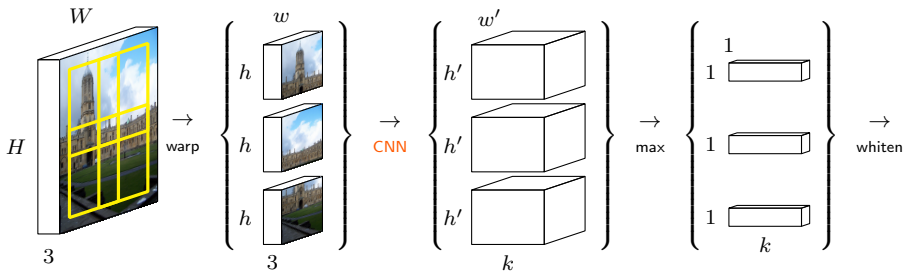
[Razavian et al. 2015]



- 3-channel RGB input, largest square region extracted
- fixed multiscale overlapping regions, **warped** into $w \times h = 227 \times 227$
- **each region** yields a $w' \times h' \times k = 36 \times 36 \times 256$ dimensional feature at the last convolutional layer of AlexNet
- global spatial **max**-pooling
- ℓ_2 -normalization, PCA-whitening of each descriptor

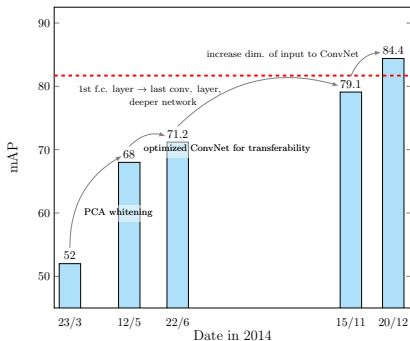
regional CNN features

[Razavian et al. 2015]



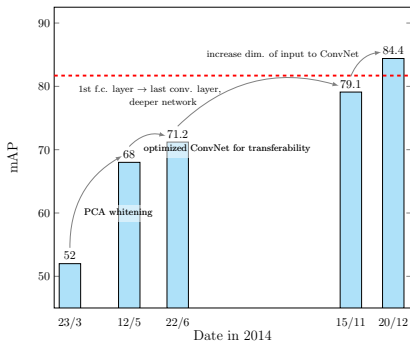
- 3-channel RGB input, largest square region extracted
- fixed multiscale overlapping regions, **warped** into $w \times h = 227 \times 227$
- **each region** yields a $w' \times h' \times k = 36 \times 36 \times 256$ dimensional feature at the last convolutional layer of AlexNet
- global spatial **max**-pooling
- ℓ_2 -normalization, PCA-whitening of each descriptor

regional CNN features



- CNN visual representation jumps by more than 30% mAP to outperform standard SIFT pipeline in a few months
- however, this is based on **multiple** regional descriptors per image and **exhaustive** pairwise matching of all descriptors of query and all dataset images, which is not practical

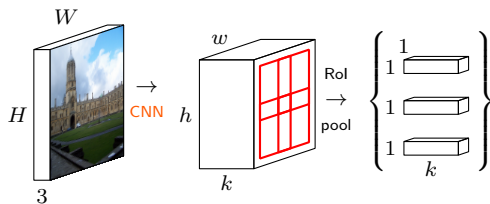
regional CNN features



- CNN visual representation jumps by more than 30% mAP to outperform standard SIFT pipeline in a few months
- however, this is based on **multiple** regional descriptors per image and **exhaustive** pairwise matching of all descriptors of query and all dataset images, which is not practical

regional max-pooling (R-MAC)

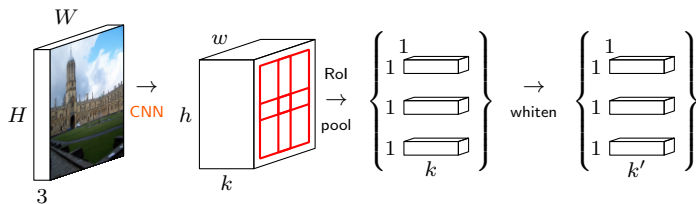
[Tolias et al. 2016]



- VGG-16 last convolutional layer, $k = 512$
- fixed multiscale overlapping regions, spatial max-pooling
- ℓ_2 -normalization, PCA-whitening, ℓ_2 -normalization
- sum-pooling over all descriptors, ℓ_2 -normalization

regional max-pooling (R-MAC)

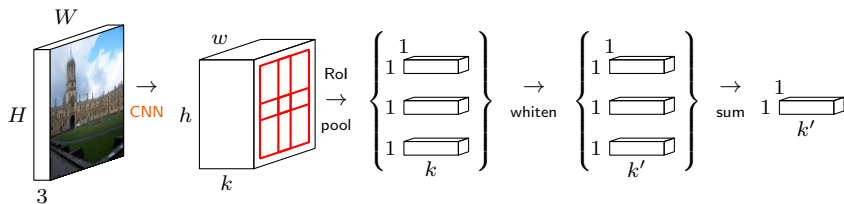
[Tolias et al. 2016]



- VGG-16 last convolutional layer, $k = 512$
- fixed multiscale overlapping regions, spatial max-pooling
- ℓ_2 -normalization, PCA-whitening, ℓ_2 -normalization
- sum-pooling over all descriptors, ℓ_2 -normalization

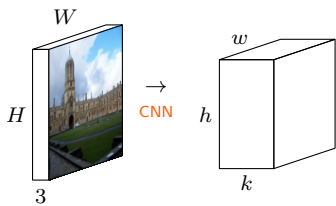
regional max-pooling (R-MAC)

[Tolias et al. 2016]



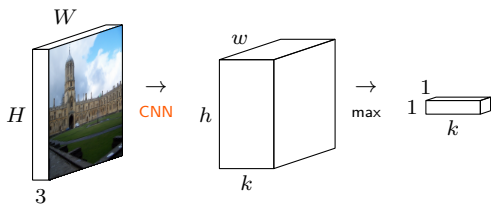
- VGG-16 last convolutional layer, $k = 512$
- fixed multiscale overlapping regions, spatial max-pooling
- ℓ_2 -normalization, PCA-whitening, ℓ_2 -normalization
- sum-pooling over all descriptors, ℓ_2 -normalization

global max-pooling (MAC)



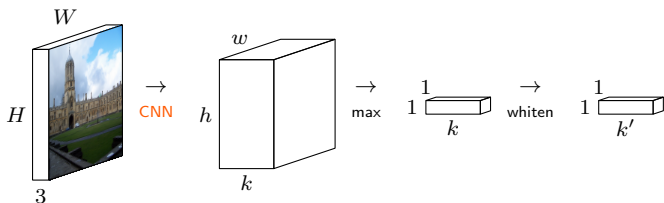
- VGG-16 last convolutional layer, $k = 512$
- global spatial max-pooling
- ℓ_2 -normalization, PCA-whitening, ℓ_2 -normalization
- MAC: maximum activation of convolutions

global max-pooling (MAC)



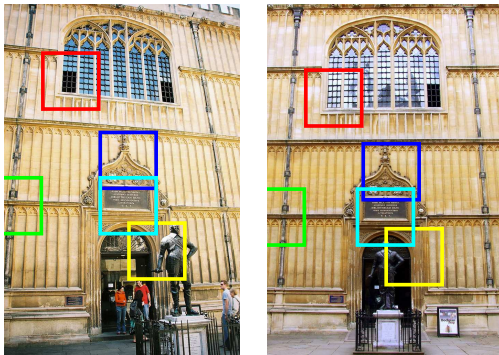
- VGG-16 last convolutional layer, $k = 512$
- global spatial **max**-pooling
- ℓ_2 -normalization, PCA-whitening, ℓ_2 -normalization
- **MAC**: maximum activation of convolutions

global max-pooling (MAC)



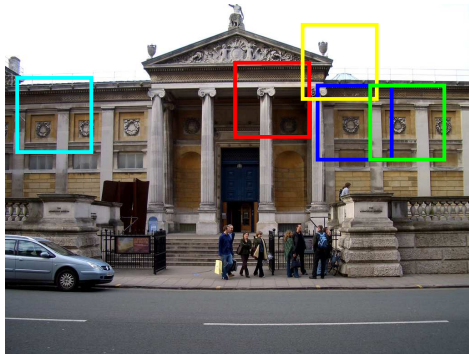
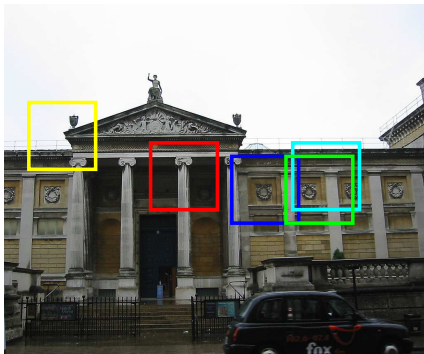
- VGG-16 last convolutional layer, $k = 512$
- global spatial **max**-pooling
- ℓ_2 -normalization, PCA-whitening, ℓ_2 -normalization
- **MAC**: maximum activation of convolutions

global max-pooling: matching



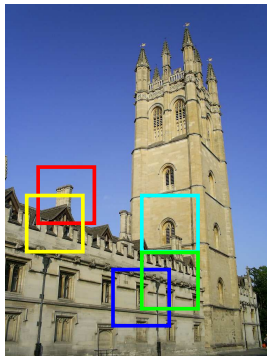
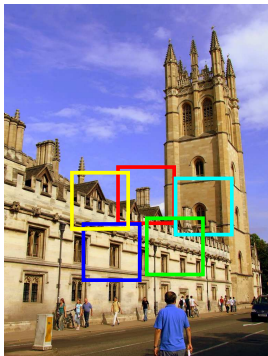
- receptive fields of 5 components of MAC vectors that contribute most to image similarity

global max-pooling: matching



- receptive fields of 5 components of MAC vectors that contribute most to image similarity

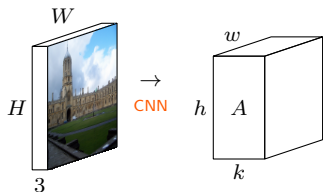
global max-pooling: matching



- receptive fields of 5 components of MAC vectors that contribute most to image similarity

cross-dimensional weighting (CroW)

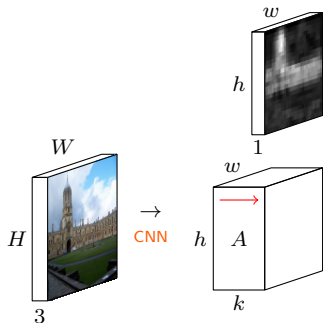
[Kalantidis et al. 2016]



- VGG-16 feature map A , last pooling layer, $k = 512$
- spatial weights F , channel weights w , weighted feature map
- global spatial sum-pooling
- ℓ_p -normalization, PCA-whitening, ℓ_2 -normalization

cross-dimensional weighting (CroW)

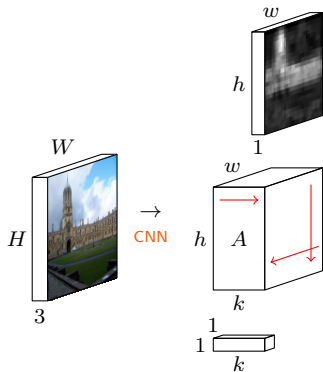
[Kalantidis et al. 2016]



- VGG-16 feature map A , last pooling layer, $k = 512$
- spatial weights F , channel weights \mathbf{w} , weighted feature map
- global spatial sum-pooling
- ℓ_p -normalization, PCA-whitening, ℓ_2 -normalization

cross-dimensional weighting (CroW)

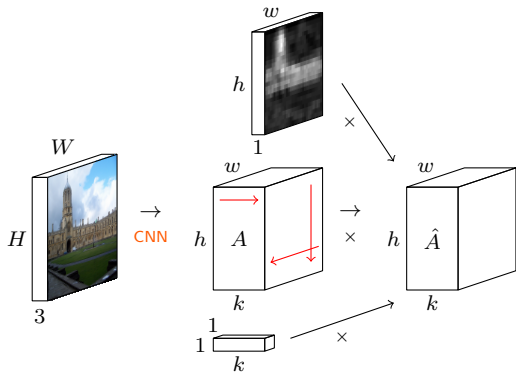
[Kalantidis et al. 2016]



- VGG-16 feature map A , last pooling layer, $k = 512$
- spatial weights F , channel weights \mathbf{w} , weighted feature map
- global spatial sum-pooling
- ℓ_p -normalization, PCA-whitening, ℓ_2 -normalization

cross-dimensional weighting (CroW)

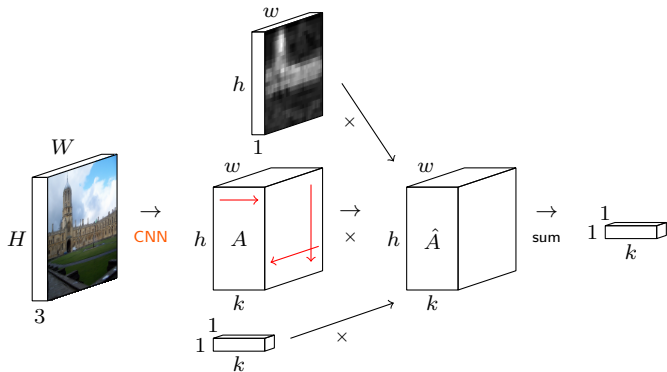
[Kalantidis et al. 2016]



- VGG-16 feature map A , last pooling layer, $k = 512$
- spatial weights F , channel weights w , weighted feature map
- global spatial sum-pooling
- ℓ_p -normalization, PCA-whitening, ℓ_2 -normalization

cross-dimensional weighting (CroW)

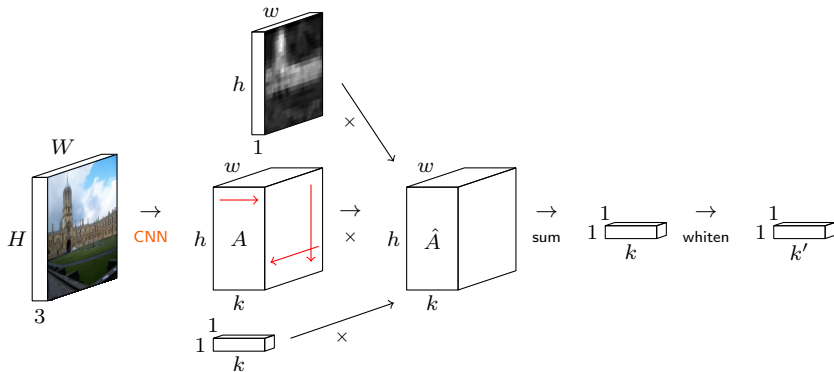
[Kalantidis et al. 2016]



- VGG-16 feature map A , last pooling layer, $k = 512$
- spatial weights F , channel weights w , weighted feature map
- global spatial sum-pooling
- ℓ_p -normalization, PCA-whitening, ℓ_2 -normalization

cross-dimensional weighting (CroW)

[Kalantidis et al. 2016]



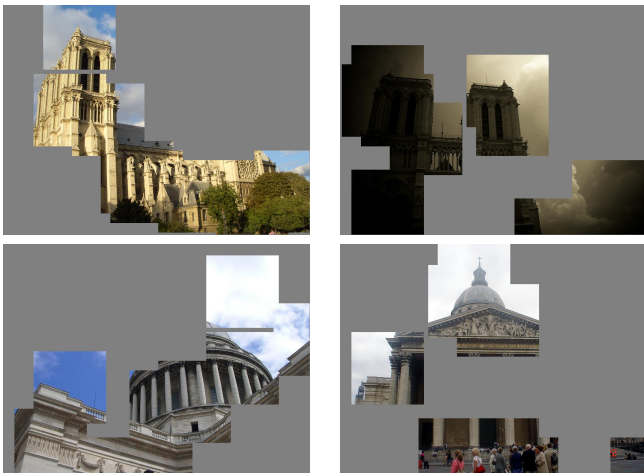
- VGG-16 feature map A , last pooling layer, $k = 512$
- spatial weights F , channel weights w , weighted feature map
- global spatial sum-pooling
- ℓ_p -normalization, PCA-whitening, ℓ_2 -normalization

cross-dimensional weighting (CroW)



- input image

cross-dimensional weighting (CroW)



- receptive fields of nonzero elements of the 10 channels with the highest sparsity-sensitive weights

manifold learning

siamese architecture

[Chopra et al. 2005]

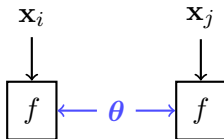
\mathbf{x}_i

\mathbf{x}_j

- an input sample is a pair $(\mathbf{x}_i, \mathbf{x}_j)$
- both $\mathbf{x}_i, \mathbf{x}_j$ go through the same function f with shared parameters θ
- loss ℓ_{ij} is measured on output pair $(\mathbf{y}_i, \mathbf{y}_j)$ and target t_{ij}

siamese architecture

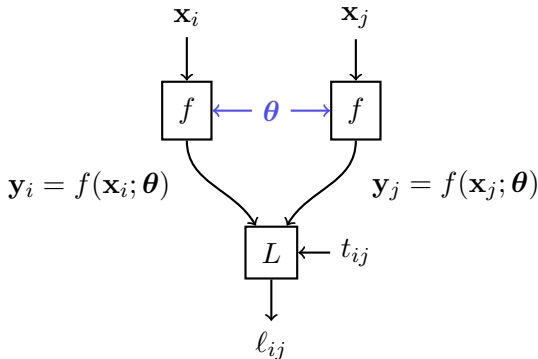
[Chopra et al. 2005]



- an input sample is a **pair** $(\mathbf{x}_i, \mathbf{x}_j)$
- both $\mathbf{x}_i, \mathbf{x}_j$ go through the **same** function f with **shared** parameters θ
- loss ℓ_{ij} is measured on output pair $(\mathbf{y}_i, \mathbf{y}_j)$ and target t_{ij}

siamese architecture

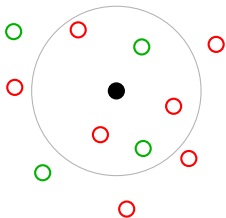
[Chopra et al. 2005]



- an input sample is a **pair** (x_i, x_j)
- both x_i, x_j go through the **same** function f with **shared** parameters θ
- loss ℓ_{ij} is measured on output pair (y_i, y_j) and target t_{ij}

contrastive loss

[Hadsel et al. 2006]



- input samples \mathbf{x}_i , output vectors $\mathbf{y}_i = f(\mathbf{x}_i; \theta)$
- target variables $t_{ij} = \mathbb{1}[\text{sim}(\mathbf{x}_i, \mathbf{x}_j)]$
- **contrastive loss** is a function of distance $\|\mathbf{y}_i - \mathbf{y}_j\|$ only

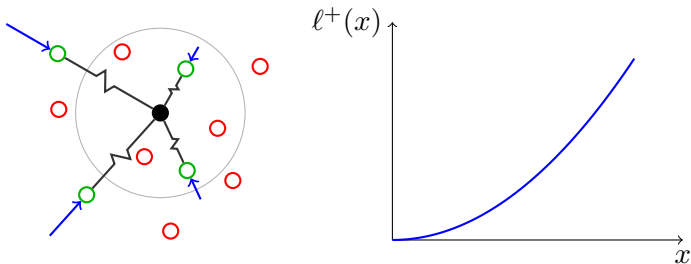
$$\ell_{ij} = L((\mathbf{y}_i, \mathbf{y}_j), t_{ij}) = \ell(\|\mathbf{y}_i - \mathbf{y}_j\|, t_{ij})$$

- **similar** samples are **attracted**

$$\ell(x, t) = t\ell^+(x) + (1 - t)\ell^-(x) = tx^2 + (1 - t)[m - x]_+^2$$

contrastive loss

[Hadsel et al. 2006]



- input samples \mathbf{x}_i , output vectors $\mathbf{y}_i = f(\mathbf{x}_i; \boldsymbol{\theta})$
- target variables $t_{ij} = \mathbb{1}[\text{sim}(\mathbf{x}_i, \mathbf{x}_j)]$
- **contrastive loss** is a function of distance $\|\mathbf{y}_i - \mathbf{y}_j\|$ only

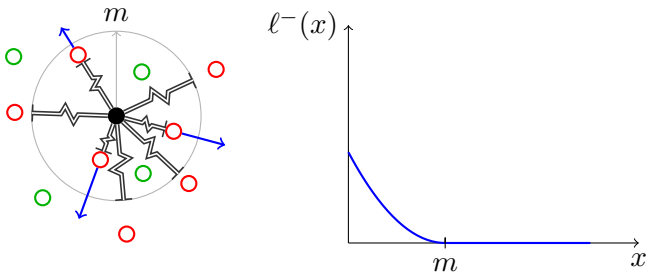
$$\ell_{ij} = L((\mathbf{y}_i, \mathbf{y}_j), t_{ij}) = \ell(\|\mathbf{y}_i - \mathbf{y}_j\|, t_{ij})$$

- **similar** samples are **attracted**

$$\ell(x, t) = t\ell^+(x) + (1 - t)\ell^-(x) = tx^2 + (1 - t)[m - x]_+^2$$

contrastive loss

[Hadsel et al. 2006]



- input samples \mathbf{x}_i , output vectors $\mathbf{y}_i = f(\mathbf{x}_i; \boldsymbol{\theta})$
- target variables $t_{ij} = \mathbb{1}[\text{sim}(\mathbf{x}_i, \mathbf{x}_j)]$
- **contrastive loss** is a function of distance $\|\mathbf{y}_i - \mathbf{y}_j\|$ only

$$\ell_{ij} = L((\mathbf{y}_i, \mathbf{y}_j), t_{ij}) = \ell(\|\mathbf{y}_i - \mathbf{y}_j\|, t_{ij})$$

- **dissimilar** samples are **repelled** if closer than **margin** m

$$\ell(x, t) = t\ell^+(x) + (1 - t)\ell^-(x) = tx^2 + (1 - t)[m - x]_+^2$$

triplet architecture

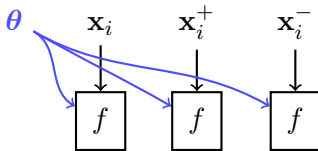
[Wang et al. 2014]

$$\mathbf{x}_i \quad \mathbf{x}_i^+ \quad \mathbf{x}_i^-$$

- an input sample is a **triplet** $(\mathbf{x}_i, \mathbf{x}_i^+, \mathbf{x}_i^-)$
- $\mathbf{x}_i, \mathbf{x}_i^+, \mathbf{x}_i^-$ go through the **same** function f with **shared** parameters θ
- loss ℓ_i measured on output triplet $(\mathbf{y}_i, \mathbf{y}_i^+, \mathbf{y}_i^-)$

triplet architecture

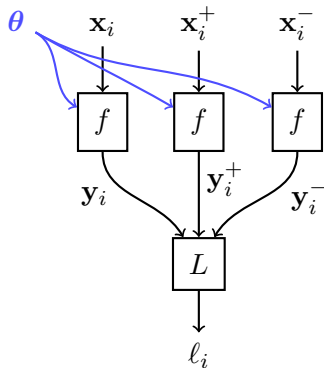
[Wang et al. 2014]



- an input sample is a **triplet** $(\mathbf{x}_i, \mathbf{x}_i^+, \mathbf{x}_i^-)$
- $\mathbf{x}_i, \mathbf{x}_i^+, \mathbf{x}_i^-$ go through the **same** function f with **shared** parameters θ
- loss ℓ_i measured on output triplet $(\mathbf{y}_i, \mathbf{y}_i^+, \mathbf{y}_i^-)$

triplet architecture

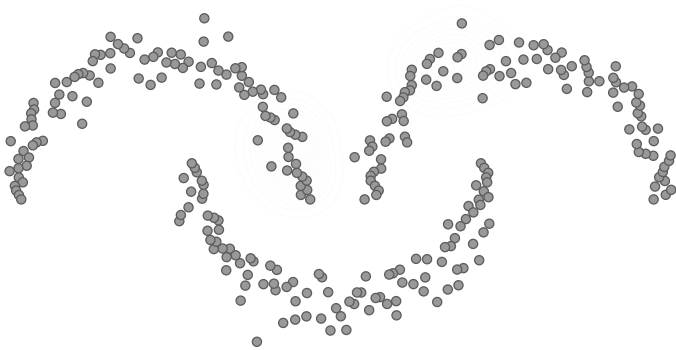
[Wang et al. 2014]



- an input sample is a **triplet** $(\mathbf{x}_i, \mathbf{x}_i^+, \mathbf{x}_i^-)$
- $\mathbf{x}_i, \mathbf{x}_i^+, \mathbf{x}_i^-$ go through the **same** function f with **shared** parameters θ
- loss ℓ_i measured on output triplet $(\mathbf{y}_i, \mathbf{y}_i^+, \mathbf{y}_i^-)$

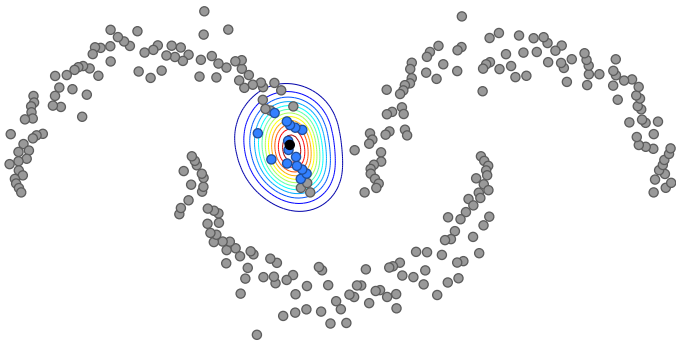
graph-based methods

ranking on manifolds: single query



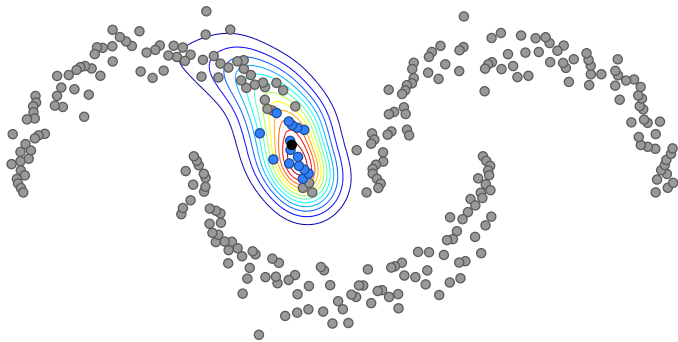
- data points (•), query point (•), nearest neighbors (•)
- iteration $\times 30$

ranking on manifolds: single query



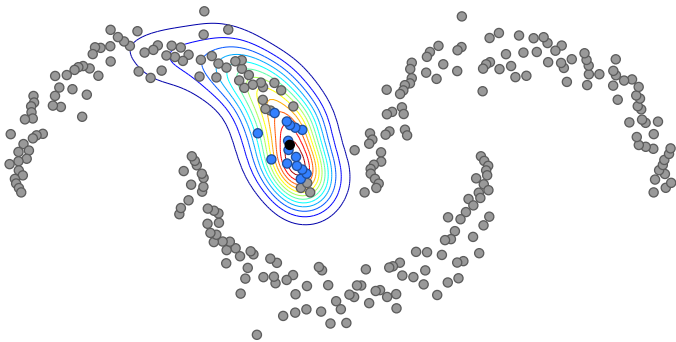
- data points (◉), query point (●), nearest neighbors (◉)
- iteration 0×30

ranking on manifolds: single query



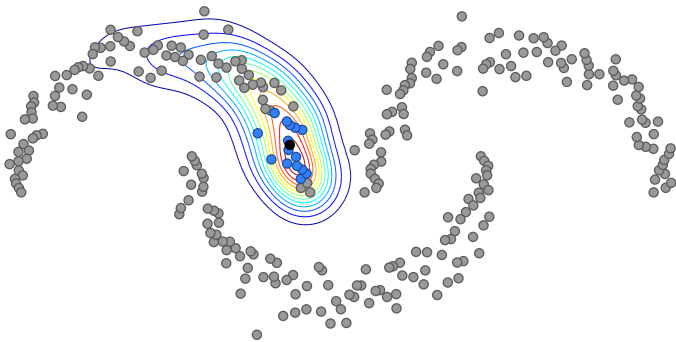
- data points (◉), query point (●), nearest neighbors (◉)
- iteration 1×30

ranking on manifolds: single query



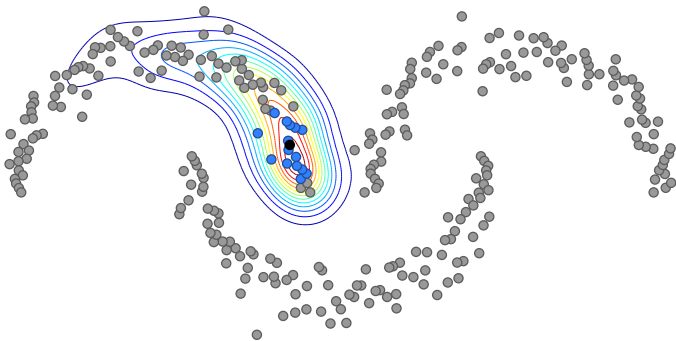
- data points (◉), query point (●), nearest neighbors (◉)
- iteration 2×30

ranking on manifolds: single query



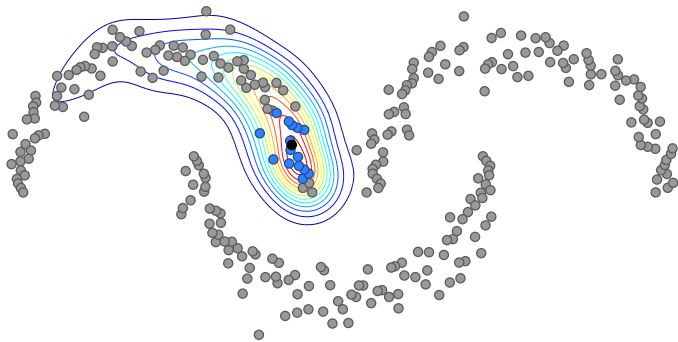
- data points (◉), query point (●), nearest neighbors (◐)
- iteration 3×30

ranking on manifolds: single query



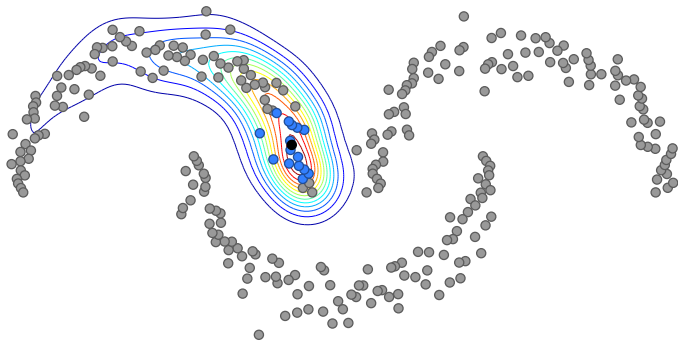
- data points (◉), query point (●), nearest neighbors (◐)
- iteration 4×30

ranking on manifolds: single query



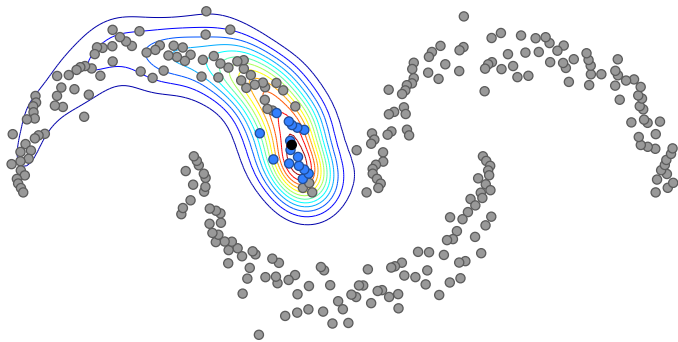
- data points (◉), query point (●), nearest neighbors (◐)
- iteration 5×30

ranking on manifolds: single query



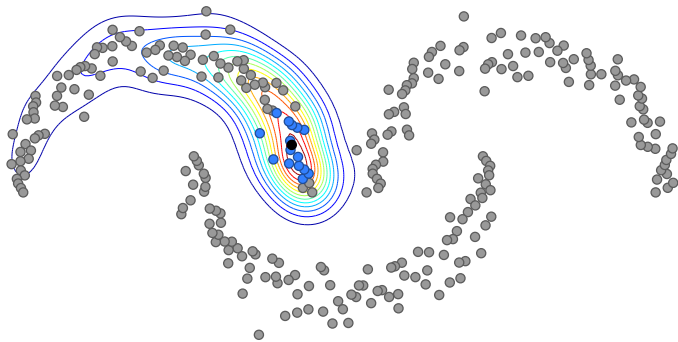
- data points (◉), query point (●), nearest neighbors (◉)
- iteration 6×30

ranking on manifolds: single query



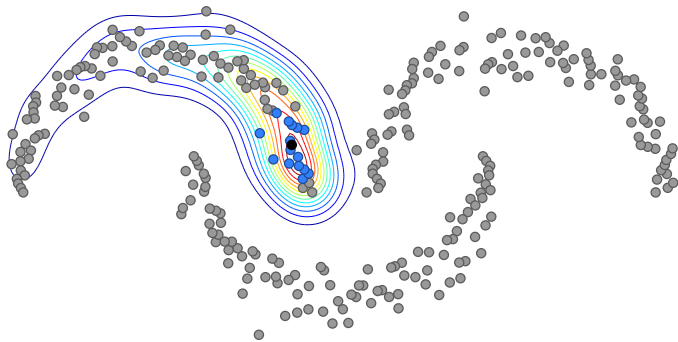
- data points (◉), query point (●), nearest neighbors (◉)
- iteration 7×30

ranking on manifolds: single query



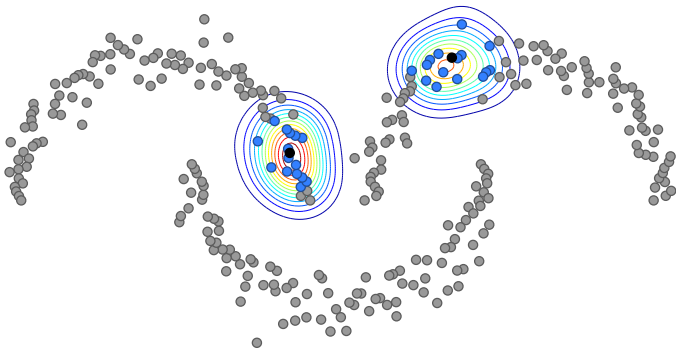
- data points (◉), query point (●), nearest neighbors (◉)
- iteration 8×30

ranking on manifolds: single query



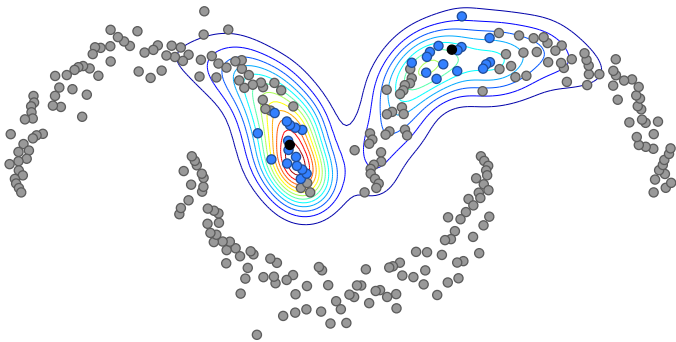
- data points (◉), query point (●), nearest neighbors (◉)
- iteration 9×30

ranking on manifolds: multiple queries



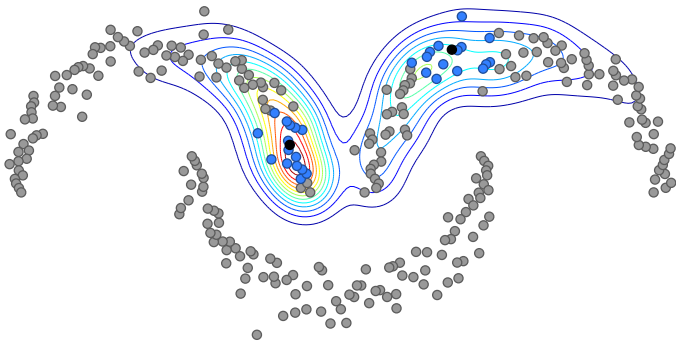
- data points (◉), query points (●), nearest neighbors (◉)
- iteration 0×30

ranking on manifolds: multiple queries



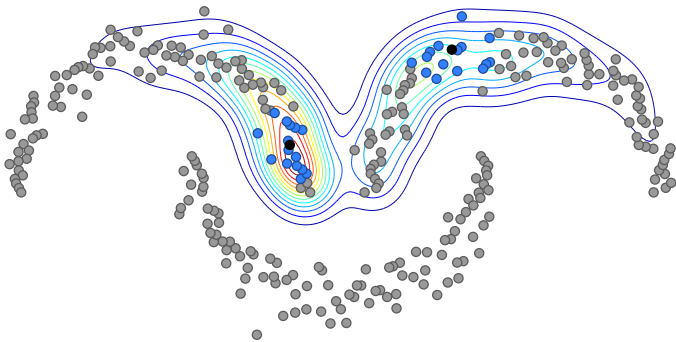
- data points (◉), query points (●), nearest neighbors (◐)
- iteration 1 × 30

ranking on manifolds: multiple queries



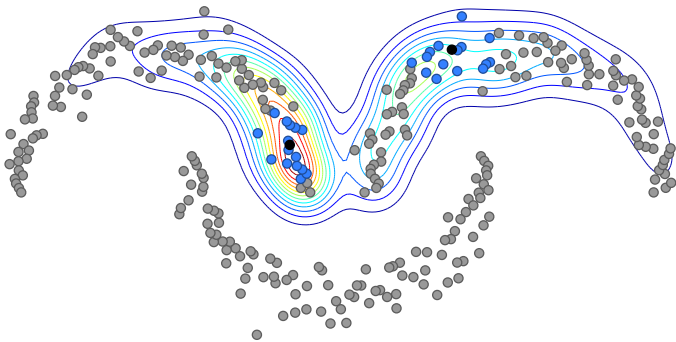
- data points (◉), query points (●), nearest neighbors (◉)
- iteration 2×30

ranking on manifolds: multiple queries



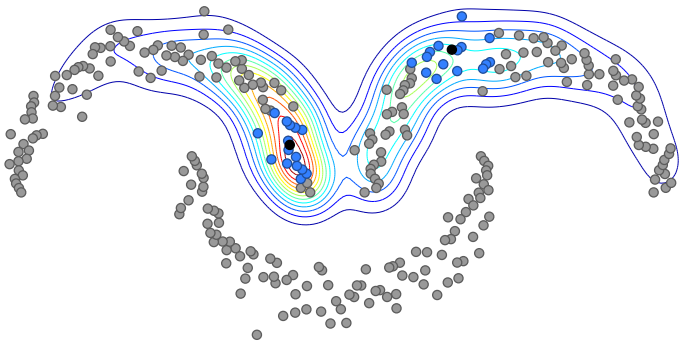
- data points (◉), query points (●), nearest neighbors (◉)
- iteration 3×30

ranking on manifolds: multiple queries



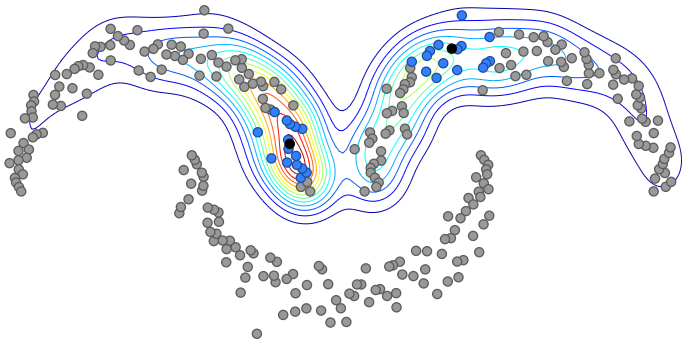
- data points (◉), query points (●), nearest neighbors (◉)
- iteration 4×30

ranking on manifolds: multiple queries



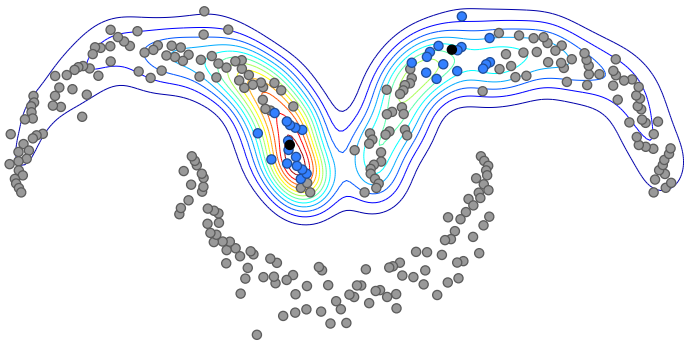
- data points (◉), query points (●), nearest neighbors (◉)
- iteration 5×30

ranking on manifolds: multiple queries



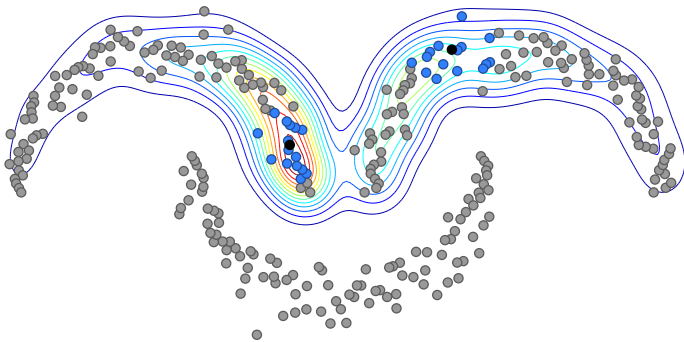
- data points (◉), query points (●), nearest neighbors (◉)
- iteration 6×30

ranking on manifolds: multiple queries



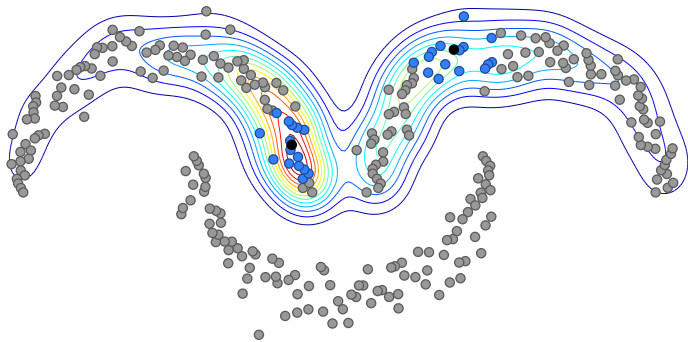
- data points (◉), query points (●), nearest neighbors (◉)
- iteration 7×30

ranking on manifolds: multiple queries



- data points (◉), query points (●), nearest neighbors (◉)
- iteration 8×30

ranking on manifolds: multiple queries



- data points (◉), query points (●), nearest neighbors (◉)
- iteration 9×30

mining on manifolds

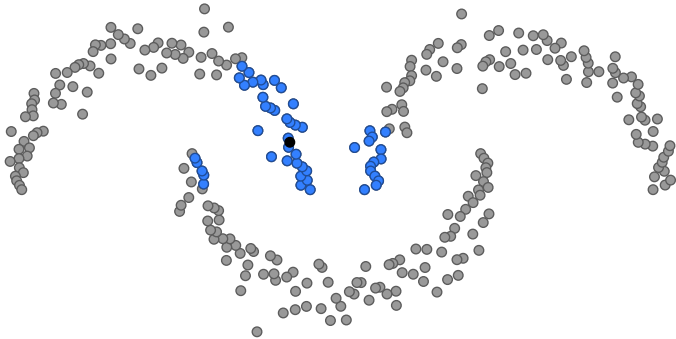
[Iscen et al. 2018]



- data points (\circ), query point x (\bullet)

mining on manifolds

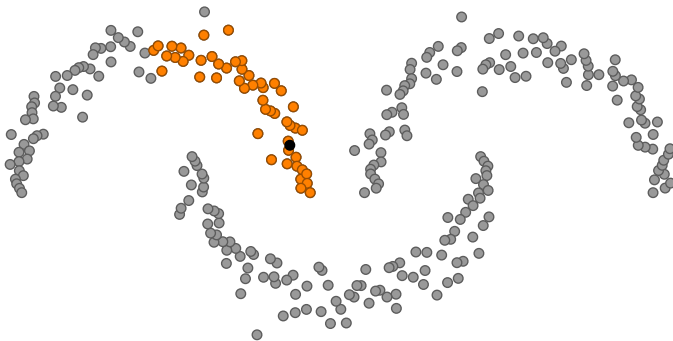
[Iscen et al. 2018]



- data points (\circ), query point x (\bullet)
- Euclidean nearest neighbors $E(x)$ (\circ)

mining on manifolds

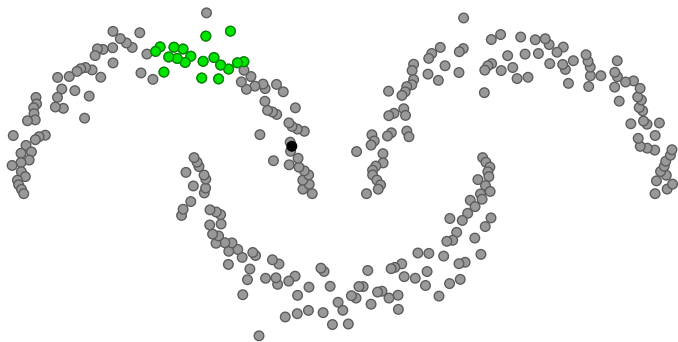
[Iscen et al. 2018]



- data points (\bullet), query point x (\bullet)
- manifold nearest neighbors $M(x)$ (\bullet)

mining on manifolds

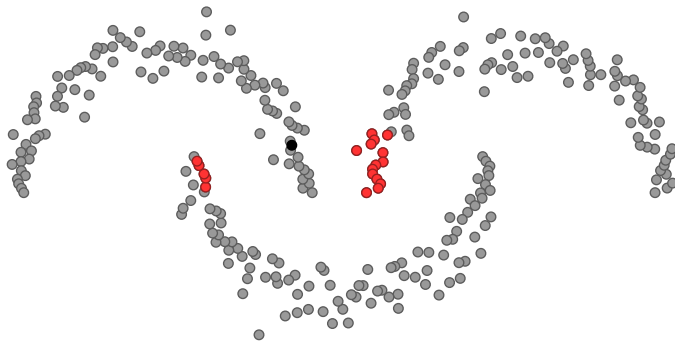
[Iscen et al. 2018]



- data points (\circ), query point \mathbf{x} (\bullet)
- **hard positives** $S^+ = M(\mathbf{x}) \setminus E(\mathbf{x})$ (\circ)

mining on manifolds

[Iscen et al. 2018]



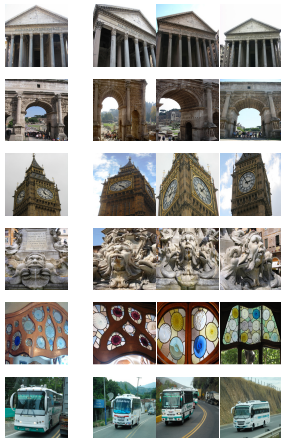
- data points (\circ), query point x (\bullet)
- **hard negatives** $S^- = E(x) \setminus M(x)$ (\bullet)

mining on manifolds



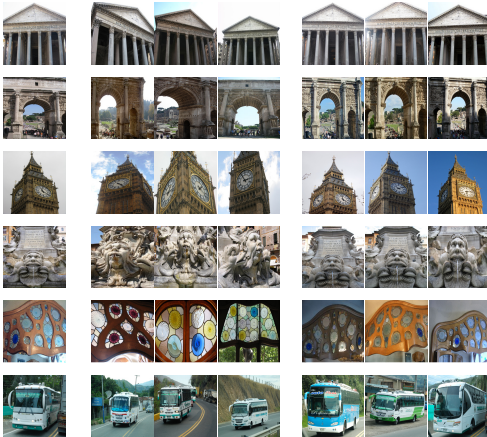
- query (anchor) (\mathbf{x})
- positives $S^+(\mathbf{x})$ vs. Euclidean neighbors $E(\mathbf{x})$
- negatives $S^-(\mathbf{x})$ vs. Euclidean non-neighbors $X \setminus E(\mathbf{x})$

mining on manifolds



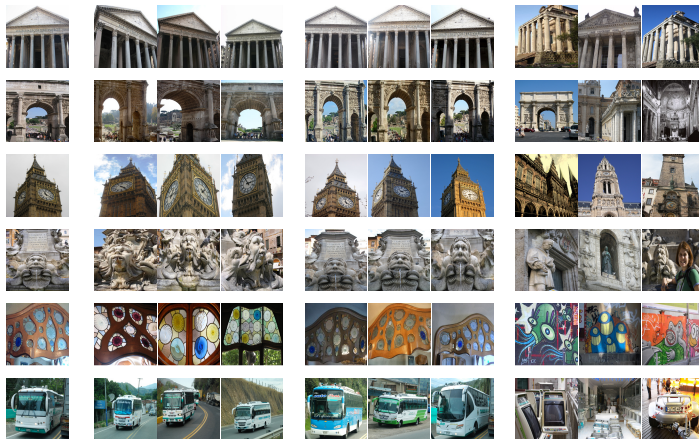
- query (anchor) (\mathbf{x})
- positives $S^+(\mathbf{x})$ vs. Euclidean neighbors $E(\mathbf{x})$
- negatives $S^-(\mathbf{x})$ vs. Euclidean non-neighbors $X \setminus E(\mathbf{x})$

mining on manifolds



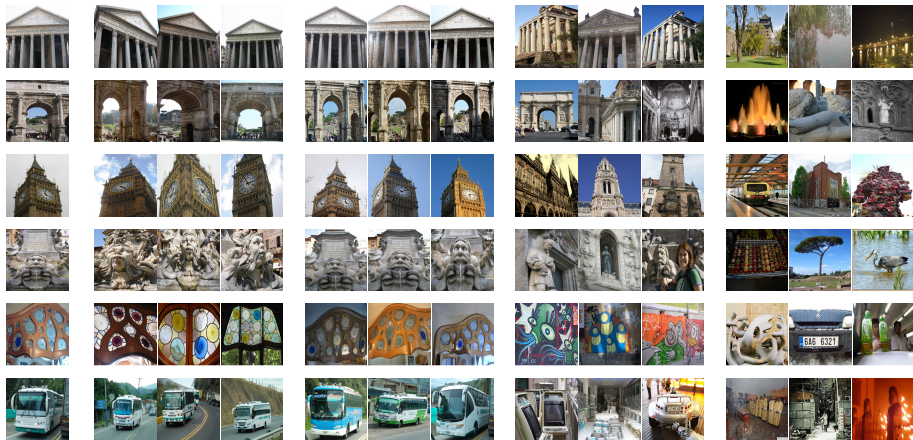
- query (anchor) (x)
- positives $S^+(x)$ vs. Euclidean neighbors $E(x)$
- negatives $S^-(x)$ vs. Euclidean non-neighbors $X \setminus E(x)$

mining on manifolds



- query (anchor) (\mathbf{x})
- positives $S^+(\mathbf{x})$ vs. Euclidean neighbors $E(\mathbf{x})$
- negatives $S^-(\mathbf{x})$ vs. Euclidean non-neighbors $X \setminus E(\mathbf{x})$

mining on manifolds



- query (anchor) (\mathbf{x})
- positives $S^+(\mathbf{x})$ vs. Euclidean neighbors $E(\mathbf{x})$
- negatives $S^-(\mathbf{x})$ vs. Euclidean non-neighbors $X \setminus E(\mathbf{x})$

Conclusion

Features and embeddings

Feature matching, geometric verification

mean Average Precision

Indexing, and approximate neighbor search

deep representation

contrastive loss

manifold learning